

# **Structural Calculation Document**

**Moss Farm Cottages  
Lower Moss Farm  
Lower Lane  
Longridge**

**Roof & Floor Timbers**

March 2023

## **Description**

The following calculations are for the new roof and floor structure at Moss Farm Cottages, Lower Moss Farm, Lower Lane, Longridge.

This document relates to the primary timber members of the floor plate and roof of the proposed cottages. All other structural items such as foundations, walls, lintels etc are to be confirmed by others.

All dimensions and details are indicative and should be checked to be suitable by on site measurement.

For all ancillary items such as wall plates, straps, joist etc, refer to the Building Regulations.

Roof Floor Timbers

**LOADING SCHEDULE**

**ROOF - PITCHED**

DEAD

Slate on Batons	0.65
Rafters	0.15
Purlins	0.10
Ceiling Joists	0.15
Insul. & P/Board	<u>0.15</u>
<b>Slope = 30 degrees</b> Total (plan)	1.39 kN/m <sup>2</sup>

IMPOSED

Roof (Snow)	<u>0.75</u>
Total	0.75 kN/m <sup>2</sup>

**FIRST FLOOR**

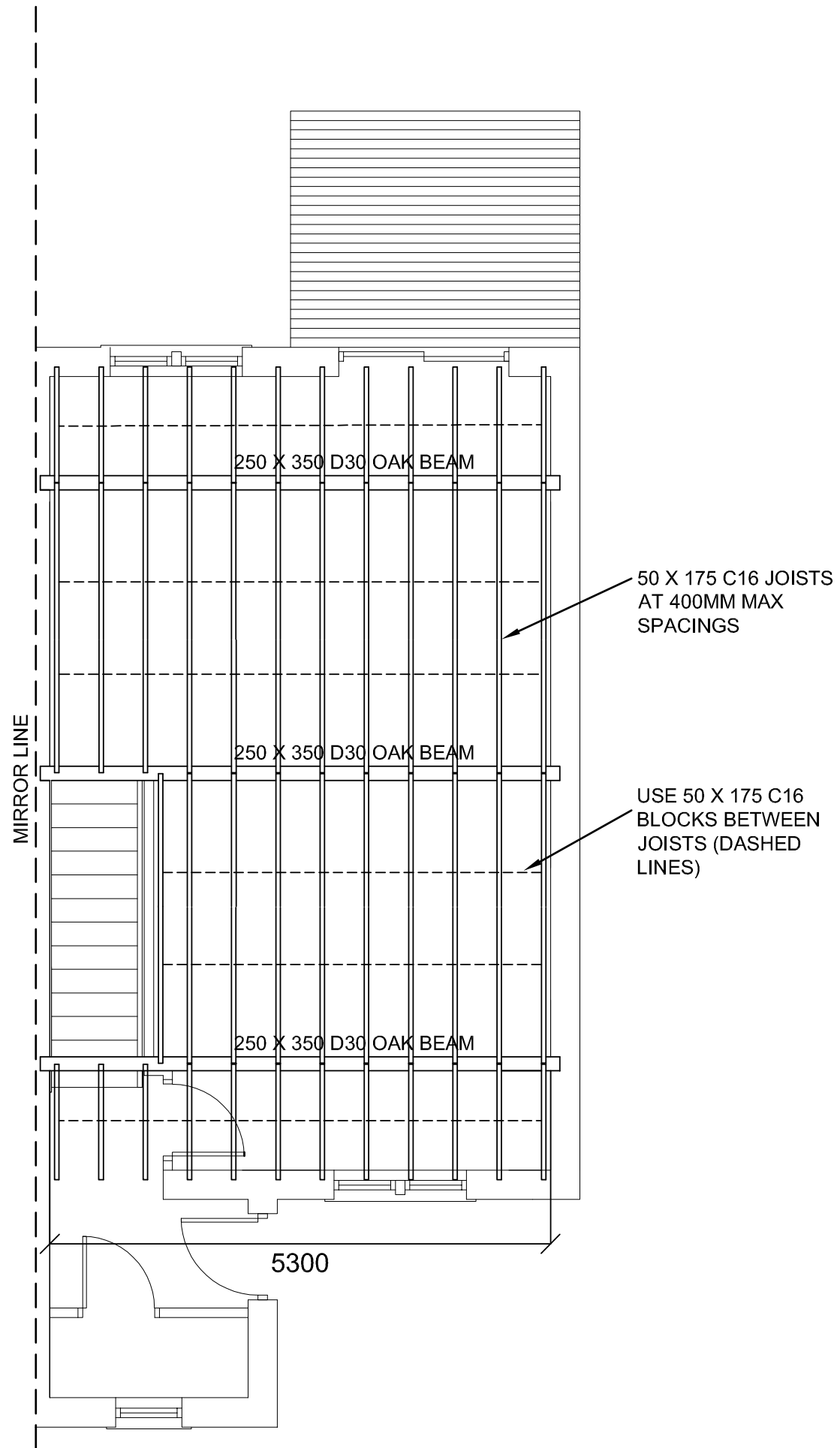
DEAD

Finishes	0.10
Chipboard	0.15
Joists	0.20
Insul. & P/Board	<u>0.15</u>
Total	0.60 kN/m <sup>2</sup>

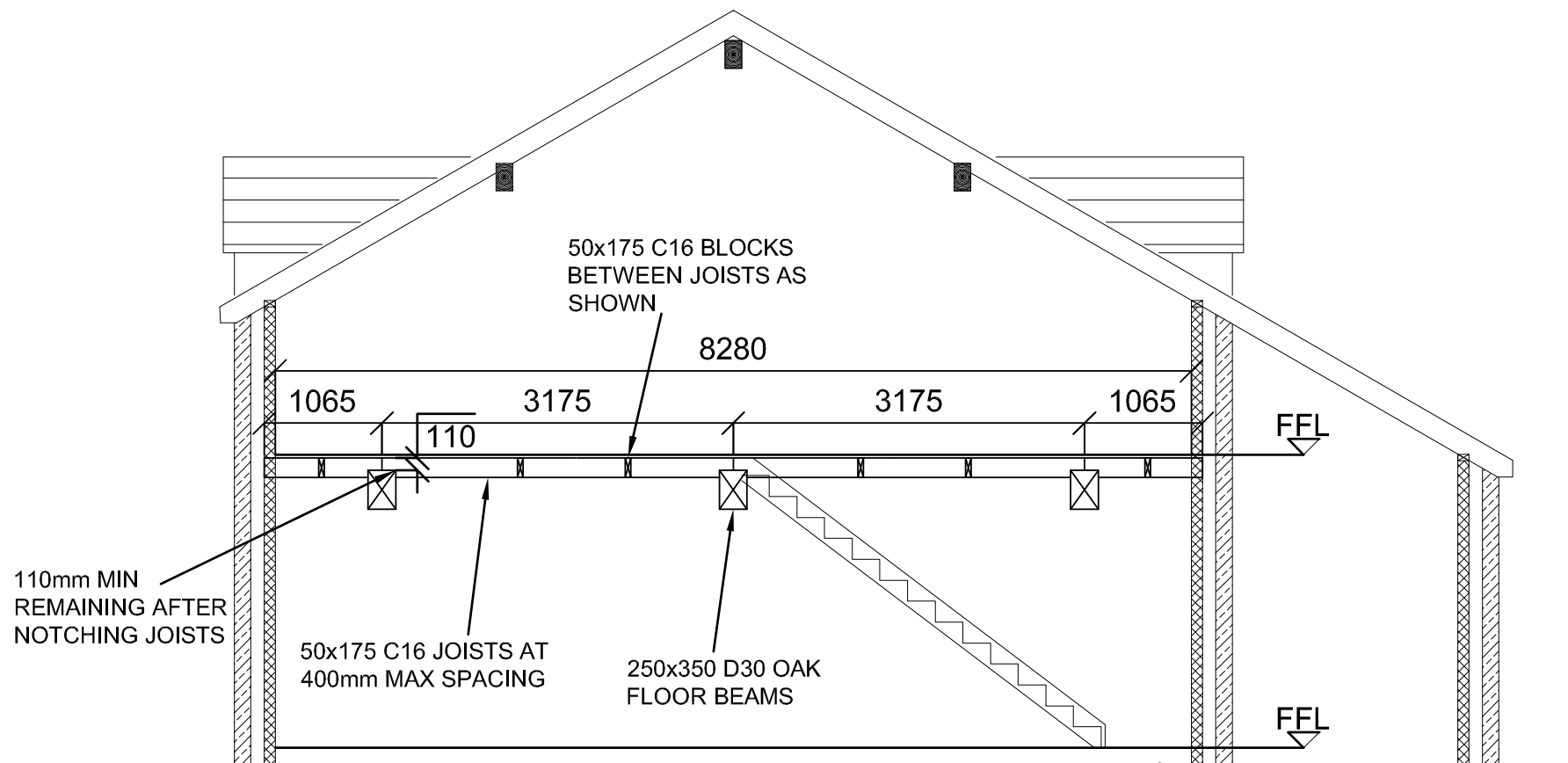
IMPOSED

Domestic	1.50
Partitions	<u>0.50</u>
Total	2.00 kN/m <sup>2</sup>

# 1ST FLOOR DESIGN



## 1ST FLOOR PLAN



## SECTION

Project <b>Moss Farm Cottages</b>				Job no.	
Calcs for <b>First Floor Joists</b>				Start page no./Revision <b>1</b>	
Calcs by <b>MC</b>	Calcs date <b>29/03/2023</b>	Checked by	Checked date	Approved by	Approved date

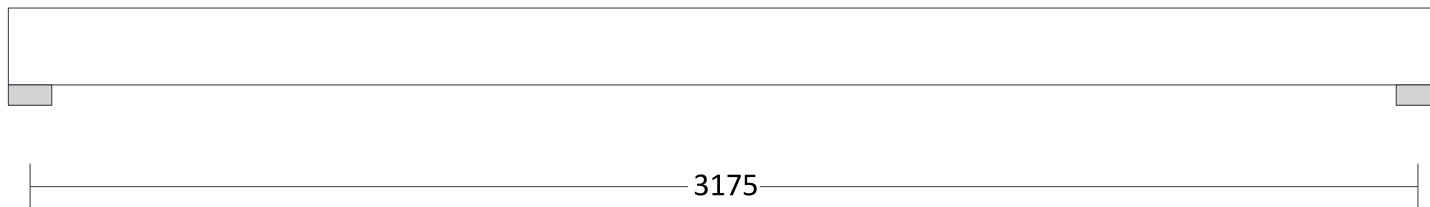
### TIMBER JOIST ANALYSIS & DESIGN (EN1995-1-1:2004)

In accordance with EN1995-1-1:2004 + A2:2014 incorporating corrigendum June 2006 and the recommended values

Tedds calculation version 1.0.04

#### Joist details

Description 47 x 175 C16 timber joists  
 Joist spacing  $s_{Joist} = 400$  mm



#### Forces input on Joist

Vertical permanent load on joist  $F_{G\_Joist} = 0.40$  kN/m<sup>2</sup>  
 Vertical imposed load on joist  $F_{Q\_Joist} = 2.00$  kN/m<sup>2</sup>

#### Joist loading details

##### Distributed loads

Vertical permanent load on joist  $p_G = F_{G\_Joist} * s_{Joist} = 0.16$  kN/m  
 Vertical imposed load on joist  $p_Q = F_{Q\_Joist} * s_{Joist} = 0.80$  kN/m

### ANALYSIS

Tedds calculation version 1.0.35

#### Loading

Self weight included (Permanent x 1)

#### Load combination factors

Load combination	Permanent	Imposed	Snow	Wind
1.35G + 1.50Q (Strength)	1.35	1.50	0.00	0.00
1.00G + 1.00Q (Service)	1.00	1.00	0.00	0.00

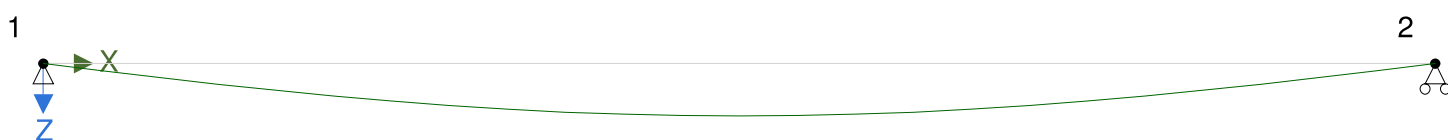
#### Member Loads

Member	Load case	Load Type	Orientation	Description
Member	Permanent	UDL	GlobalZ	0.16 kN/m at 0 m to 3.175 m
Member	Imposed	UDL	GlobalZ	0.8 kN/m at 0 m to 3.175 m

### Results

#### Total deflection

1.35G + 1.50Q (Strength) - Total deflection



Project		Moss Farm Cottages		Job no.	
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				2	
Calcs by	Calcs date	Checked by	Checked date	Approved by	Approved date
MC	29/03/2023				

**1.00G + 1.00Q (Service) - Total deflection**



**Node deflections**

**Load combination: 1.35G + 1.50Q (Strength)**

Node	Deflection		Rotation (°)	Co-ordinate system
	X (mm)	Z (mm)		
1	0	0	0.65965	
2	0	0	-0.65965	

**Load combination: 1.00G + 1.00Q (Service)**

Node	Deflection		Rotation (°)	Co-ordinate system
	X (mm)	Z (mm)		
1	0	0	0.44819	
2	0	0	-0.44819	

**Total base reactions**

Load case/combination	Force	
	FX (kN)	FZ (kN)
1.35G + 1.50Q (Strength)	0	4.6
1.00G + 1.00Q (Service)	0	3.1

**Element end forces**

**Load combination: 1.35G + 1.50Q (Strength)**

Element	Length (m)	Nodes Start/End	Axial force (kN)	Shear force (kN)	Moment (kNm)
1	3.175	1	0	-2.3	0
		2	0	-2.3	0

**Load combination: 1.00G + 1.00Q (Service)**

Element	Length (m)	Nodes Start/End	Axial force (kN)	Shear force (kN)	Moment (kNm)
1	3.175	1	0	-1.6	0
		2	0	-1.6	0

**Forces**

**Strength combinations - Moment envelope (kNm)**



Project <b>Moss Farm Cottages</b>				Job no.	
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### Strength combinations - Shear envelope (kN)



### Member results

#### Envelope - Strength combinations

Member	Position (m)	Shear force (kN)	Moment (kNm)
Member	0	2.3 (max abs)	0 (min)
	1.588	0	1.8 (max)
	3.175	-2.3	0 (min)

Tedds calculation version 2.2.07

### Member - Span 1

#### Partial factor for material properties and resistances

Partial factor for material properties - Table 2.3  $\gamma_M = 1.300$

#### Member details

Load duration - cl.2.3.1.2 Medium-term

Service class - cl.2.3.1.3 1

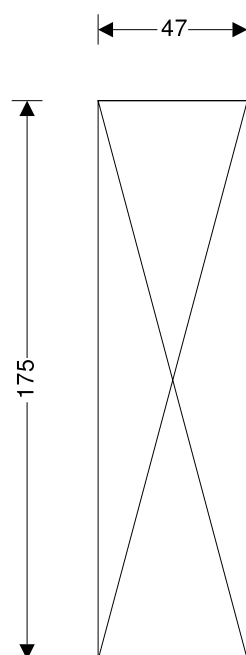
#### Timber section details

Number of timber sections in member  $N = 1$

Breadth of sections  $b = 47$  mm

Depth of sections  $h = 175$  mm

Timber strength class - EN 338:2016 Table 1 **C16**



#### 47x175 timber section

Cross-sectional area,  $A$ , 8225 mm<sup>2</sup>

Section modulus,  $W_y$ , 239895.8 mm<sup>3</sup>

Section modulus,  $W_z$ , 64429 mm<sup>3</sup>

Second moment of area,  $I_y$ , 20990885 mm<sup>4</sup>

Second moment of area,  $I_z$ , 1514085 mm<sup>4</sup>

Radius of gyration,  $i_y$ , 50.5 mm

Radius of gyration,  $i_z$ , 13.6 mm

#### Timber strength class C16

Characteristic bending strength,  $f_{m,k}$ , 16 N/mm<sup>2</sup>

Characteristic shear strength,  $f_{v,k}$ , 3.2 N/mm<sup>2</sup>

Characteristic compression strength parallel to grain,  $f_{c,0,k}$ , 17 N/mm<sup>2</sup>

Characteristic compression strength perpendicular to grain,  $f_{c,90,k}$ , 2.2 N/mm<sup>2</sup>

Characteristic tension strength parallel to grain,  $f_{t,0,k}$ , 8.5 N/mm<sup>2</sup>

Mean modulus of elasticity,  $E_{0,mean}$ , 8000 N/mm<sup>2</sup>

Fifth percentile modulus of elasticity,  $E_{0,05}$ , 5400 N/mm<sup>2</sup>

Shear modulus of elasticity,  $G_{mean}$ , 500 N/mm<sup>2</sup>

Characteristic density,  $\rho_k$ , 310 kg/m<sup>3</sup>

Mean density,  $\rho_{mean}$ , 370 kg/m<sup>3</sup>

Project <b>Moss Farm Cottages</b>				Job no.	
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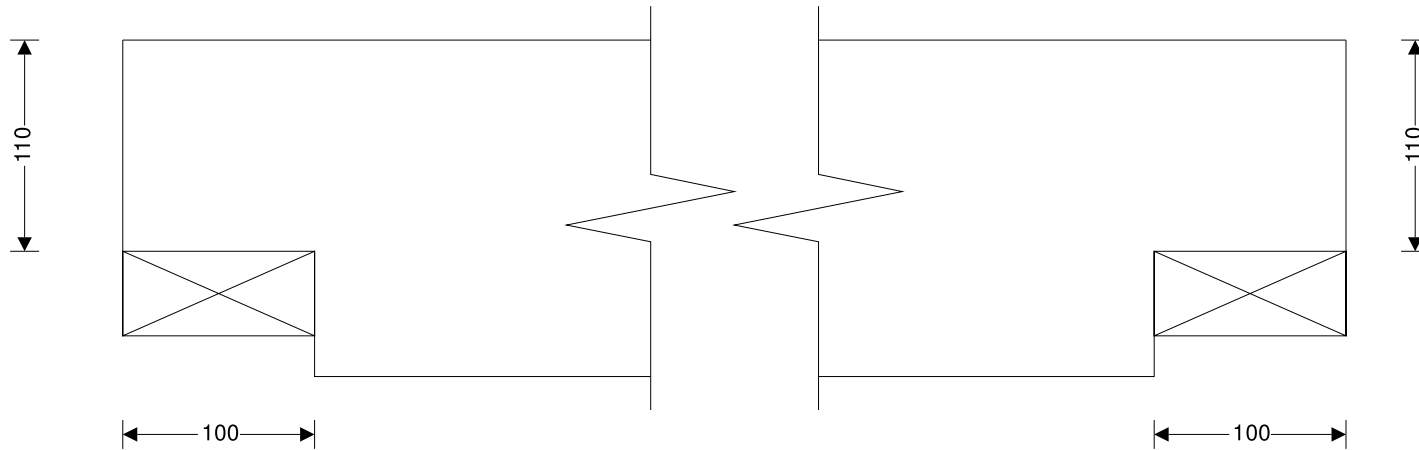
### Span details

Bearing length

$$L_b = 100 \text{ mm}$$

Depth at notched end

$$h_{ef} = 110 \text{ mm}$$



### Consider Combination 1 - 1.35G + 1.50Q (Strength)

#### Modification factors

Duration of load and moisture content - Table 3.1  $k_{mod} = 0.8$

Deformation factor - Table 3.2  $k_{def} = 0.6$

Bending stress re-distribution factor - cl.6.1.6(2)  $k_m = 0.7$

Crack factor for shear resistance - cl.6.1.7(2)  $k_{cr} = 0.67$

System strength factor - cl.6.6  $k_{sys} = 1.1$

Notch inclination  $i_n = 0$

Distance from support reaction to corner of notch  $x_n = L_b / 2 + L_x = 50 \text{ mm}$

Material factor - exp.6.63  $k_n = 5$

Member end depth ratio  $\alpha_n = h_{ef} / h = 0.629$

Notch reduction factor - exp.6.62

$$k_v = \min(1, k_n * (1 + 1.1 * i_n^{1.5} / \sqrt{(h / 1 \text{ mm})}) / (\sqrt{(h / 1 \text{ mm})} * (\sqrt{(\alpha_n * (1 - \alpha_n)) + 0.8 * x_n / h * \sqrt{(1 / \alpha_n - \alpha_n^2))}})) = 0.516$$

### Check design at start of span

#### Check compression perpendicular to the grain - cl.6.1.5

Design perpendicular compression - major axis  $F_{c,y,90,d} = 2.301 \text{ kN}$

Effective contact length  $L_{b,ef} = L_b = 100 \text{ mm}$

Design perpendicular compressive stress - exp.6.4  $\sigma_{c,y,90,d} = F_{c,y,90,d} / (b * L_{b,ef}) = 0.490 \text{ N/mm}^2$

Design perpendicular compressive strength  $f_{c,y,90,d} = k_{mod} * k_{sys} * f_{c,90,k} / \gamma_M = 1.489 \text{ N/mm}^2$

$$\sigma_{c,y,90,d} / (k_{c,90} * f_{c,y,90,d}) = 0.329$$

**PASS - Design perpendicular compression strength exceeds design perpendicular compression stress**

#### Check shear force - Section 6.1.7

Design shear force  $F_{y,d} = 2.301 \text{ kN}$

Design shear stress - exp.6.60  $\tau_{y,d} = 1.5 * F_{y,d} / (k_{cr} * b * h_{ef}) = 0.997 \text{ N/mm}^2$

Design shear strength  $f_{v,y,d} = k_{mod} * k_{sys} * f_{v,k} / \gamma_M = 2.166 \text{ N/mm}^2$

$$\tau_{y,d} / (k_v * f_{v,y,d}) = 0.892$$

**PASS - Design shear strength exceeds design shear stress**

### Check design 1588 mm along span

#### Check bending moment - Section 6.1.6

Design bending moment  $M_{y,d} = 1.827 \text{ kNm}$

Design bending stress  $\sigma_{m,y,d} = M_{y,d} / W_y = 7.615 \text{ N/mm}^2$

Project <b>Moss Farm Cottages</b>				Job no.	
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Design bending strength

$$f_{m,y,d} = k_{mod} * k_{sys} * f_{m,k} / \gamma_M = \mathbf{10.831 \text{ N/mm}^2}$$

$$\sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.703}$$

**PASS - Design bending strength exceeds design bending stress**

**Check design at end of span**

**Check compression perpendicular to the grain - cl.6.1.5**

Design perpendicular compression - major axis  $F_{c,y,90,d} = \mathbf{2.301 \text{ kN}}$

Effective contact length  $L_{b,ef} = L_b = \mathbf{100 \text{ mm}}$

Design perpendicular compressive stress - exp.6.4  $\sigma_{c,y,90,d} = F_{c,y,90,d} / (b * L_{b,ef}) = \mathbf{0.490 \text{ N/mm}^2}$

Design perpendicular compressive strength  $f_{c,y,90,d} = k_{mod} * k_{sys} * f_{c,90,k} / \gamma_M = \mathbf{1.489 \text{ N/mm}^2}$

$$\sigma_{c,y,90,d} / (k_{c,90} * f_{c,y,90,d}) = \mathbf{0.329}$$

**PASS - Design perpendicular compression strength exceeds design perpendicular compression stress**

**Check shear force - Section 6.1.7**

Design shear force  $F_{y,d} = \mathbf{2.301 \text{ kN}}$

Design shear stress - exp.6.60  $\tau_{y,d} = 1.5 * F_{y,d} / (k_{cr} * b * h_{ef}) = \mathbf{0.997 \text{ N/mm}^2}$

Design shear strength  $f_{v,y,d} = k_{mod} * k_{sys} * f_{v,k} / \gamma_M = \mathbf{2.166 \text{ N/mm}^2}$

$$\tau_{y,d} / (k_v * f_{v,y,d}) = \mathbf{0.892}$$

**PASS - Design shear strength exceeds design shear stress**

**Consider Combination 2 - 1.00G + 1.00Q (Service)**

**Check design 1587 mm along span**

**Check y-y axis deflection - Section 7.2**

Instantaneous deflection  $\delta_y = \mathbf{8.1 \text{ mm}}$

Allowable deflection  $\delta_{y,Allowable} = L_{m1_s1} / 250 = \mathbf{12.7 \text{ mm}}$

$$\delta_y / \delta_{y,Allowable} = \mathbf{0.64}$$

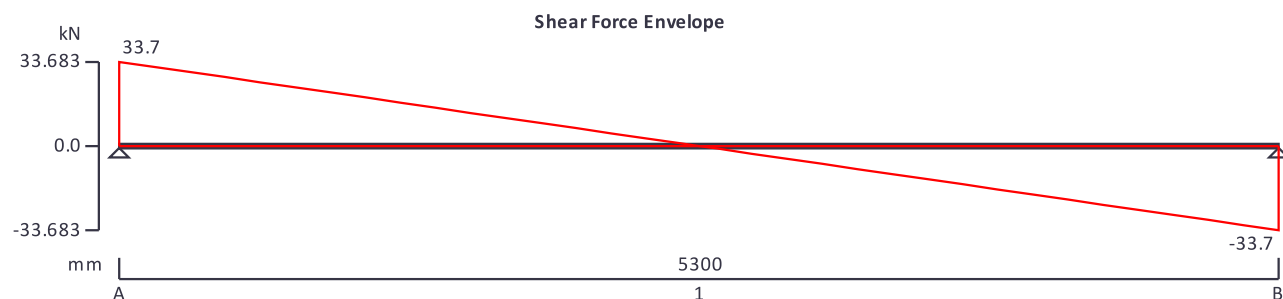
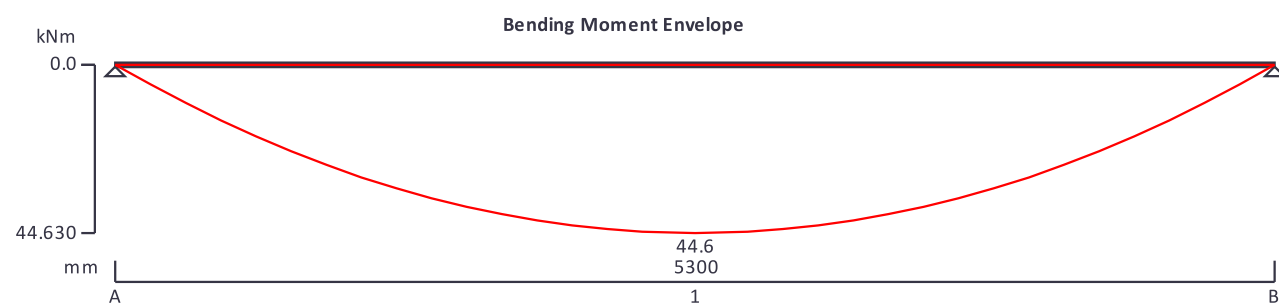
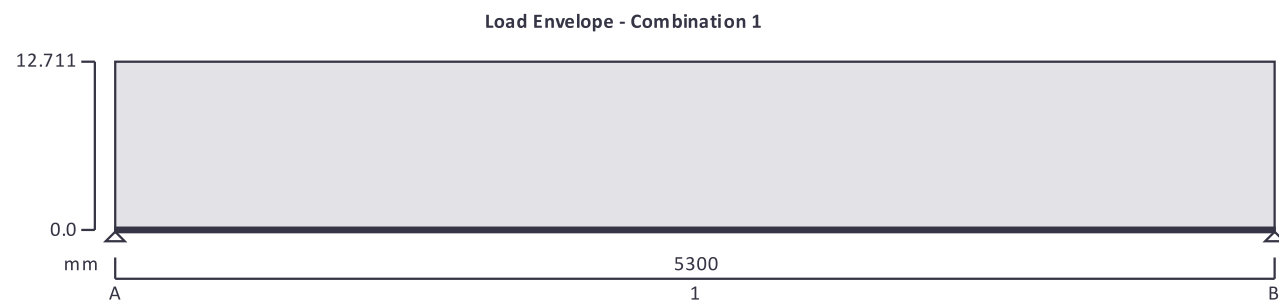
**PASS - Allowable deflection exceeds final deflection**

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Calcs for <b>Oak Floor Beams</b>				Start page no./Revision <b>1</b>	
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### TIMBER BEAM ANALYSIS & DESIGN TO EN1995-1-1:2004

In accordance with EN1995-1-1:2004 + A2:2014 and Corrigendum No.1 and the UK National Annex incorporating National Amendment No.1

Tedds calculation version 1.7.04



#### Applied loading

##### Beam loads

Dead

Permanent self weight of beam \* 1

Imposed

Permanent full UDL 1.905 kN/m

Variable full UDL 6.350 kN/m

##### Load combinations

Load combination 1

Support A

Permanent \* 1.35

Variable \* 1.50

Span 1

Permanent \* 1.35

Variable \* 1.50

Support B

Permanent \* 1.35

Variable \* 1.50

##### Analysis results

Maximum moment

$M_{max} = 44.630$  kNm

$M_{min} = 0.000$  kNm

Design moment

$M = \max(\text{abs}(M_{max}), \text{abs}(M_{min})) = 44.630$  kNm

Maximum shear

$F_{max} = 33.683$  kN

$F_{min} = -33.683$  kN

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Design shear

$$F = \max(\text{abs}(F_{\max}), \text{abs}(F_{\min})) = \mathbf{33.683 \text{ kN}}$$

Total load on beam

$$W_{\text{tot}} = \mathbf{67.367 \text{ kN}}$$

Reactions at support A

$$R_{A_{\max}} = \mathbf{33.683 \text{ kN}}$$

$$R_{A_{\min}} = \mathbf{33.683 \text{ kN}}$$

Unfactored permanent load reaction at support A

$$R_{A_{\text{Permanent}}} = \mathbf{6.253 \text{ kN}}$$

Unfactored variable load reaction at support A

$$R_{A_{\text{Variable}}} = \mathbf{16.828 \text{ kN}}$$

Reactions at support B

$$R_{B_{\max}} = \mathbf{33.683 \text{ kN}}$$

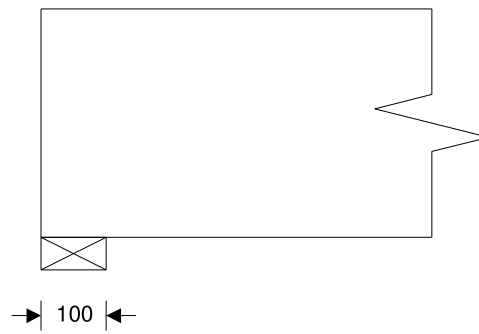
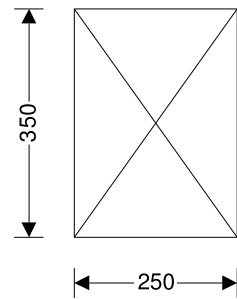
$$R_{B_{\min}} = \mathbf{33.683 \text{ kN}}$$

Unfactored permanent load reaction at support B

$$R_{B_{\text{Permanent}}} = \mathbf{6.253 \text{ kN}}$$

Unfactored variable load reaction at support B

$$R_{B_{\text{Variable}}} = \mathbf{16.828 \text{ kN}}$$



### Timber section details

Breadth of timber sections

$$b = \mathbf{250 \text{ mm}}$$

Depth of timber sections

$$h = \mathbf{350 \text{ mm}}$$

Number of timber sections in member

$$N = \mathbf{1}$$

Overall breadth of timber member

$$b_b = N \times b = \mathbf{250 \text{ mm}}$$

Timber strength class - EN 338:2016 Table 3

**D30**

### Member details

Load duration - cl.2.3.1.2

**Medium-term**

Service class of timber - cl.2.3.1.3

**1**

Length of span

$$L_{s1} = \mathbf{5300 \text{ mm}}$$

Length of bearing

$$L_b = \mathbf{100 \text{ mm}}$$

### Section properties

Cross sectional area of member

$$A = N \times b \times h = \mathbf{87500 \text{ mm}^2}$$

Section modulus

$$W_y = N \times b \times h^2 / 6 = \mathbf{5104167 \text{ mm}^3}$$

$$W_z = h \times (N \times b)^2 / 6 = \mathbf{3645833 \text{ mm}^3}$$

Second moment of area

$$I_y = N \times b \times h^3 / 12 = \mathbf{893229167 \text{ mm}^4}$$

$$I_z = h \times (N \times b)^3 / 12 = \mathbf{455729167 \text{ mm}^4}$$

Radius of gyration

$$r_y = \sqrt{I_y / A} = \mathbf{101.0 \text{ mm}}$$

$$r_z = \sqrt{I_z / A} = \mathbf{72.2 \text{ mm}}$$

### Partial factor for material properties and resistances

Partial factor for material properties - Table 2.3

$$\gamma_M = \mathbf{1.300}$$

### Modification factors

Modification factor for load duration and moisture content - Table 3.1

$$k_{\text{mod}} = \mathbf{0.800}$$

Deformation factor for service classes - Table 3.2

$$k_{\text{def}} = \mathbf{0.600}$$

Depth factor for bending - exp.3.1

$$k_{h,m} = \mathbf{1.000}$$

Depth factor for tension - exp.3.1

$$k_{h,t} = \mathbf{1.000}$$

Bending stress re-distribution factor - cl.6.1.6(2)

$$k_m = \mathbf{0.700}$$

Crack factor for shear resistance - cl.6.1.7(2)

$$k_{\text{cr}} = \mathbf{0.670}$$

Load configuration factor - exp.6.4

$$k_{c,90} = \mathbf{1.000}$$

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System strength factor - cl.6.6

$$k_{sys} = \mathbf{1.000}$$

Lateral buckling factor - cl.6.3.3(5)

$$k_{crit} = \mathbf{1.000}$$

### Compression perpendicular to the grain - cl.6.1.5

Design compressive stress

$$\sigma_{c,90,d} = R_{A,max} / (N * b * L_b) = \mathbf{1.347 \text{ N/mm}^2}$$

Design compressive strength

$$f_{c,90,d} = k_{mod} * k_{sys} * k_{c,90} * f_{c,90,k} / \gamma_M = \mathbf{3.262 \text{ N/mm}^2}$$

$$\sigma_{c,90,d} / f_{c,90,d} = \mathbf{0.413}$$

**PASS - Design compressive strength exceeds design compressive stress at bearing**

### Bending - cl 6.1.6

Design bending stress

$$\sigma_{m,d} = M / W_y = \mathbf{8.744 \text{ N/mm}^2}$$

Design bending strength

$$f_{m,d} = k_{h,m} * k_{mod} * k_{sys} * k_{crit} * f_{m,k} / \gamma_M = \mathbf{18.462 \text{ N/mm}^2}$$

$$\sigma_{m,d} / f_{m,d} = \mathbf{0.474}$$

**PASS - Design bending strength exceeds design bending stress**

### Shear - cl.6.1.7

Applied shear stress

$$\tau_d = 3 * F / (2 * k_{cr} * A) = \mathbf{0.862 \text{ N/mm}^2}$$

Permissible shear stress

$$f_{v,d} = k_{mod} * k_{sys} * f_{v,k} / \gamma_M = \mathbf{2.400 \text{ N/mm}^2}$$

$$\tau_d / f_{v,d} = \mathbf{0.359}$$

**PASS - Design shear strength exceeds design shear stress**

### Deflection - cl.7.2

Deflection limit

$$\delta_{lim} = \min(14 \text{ mm}, 0.004 * L_{s1}) = \mathbf{14.000 \text{ mm}}$$

Instantaneous deflection due to permanent load

$$\delta_{instG} = \mathbf{2.632 \text{ mm}}$$

Final deflection due to permanent load

$$\delta_{finG} = \delta_{instG} * (1 + k_{def}) = \mathbf{4.212 \text{ mm}}$$

Instantaneous deflection due to variable load

$$\delta_{instQ} = \mathbf{7.083 \text{ mm}}$$

Factor for quasi-permanent variable action

$$\psi_2 = \mathbf{0.3}$$

Final deflection due to variable load

$$\delta_{finQ} = \delta_{instQ} * (1 + \psi_2 * k_{def}) = \mathbf{8.358 \text{ mm}}$$

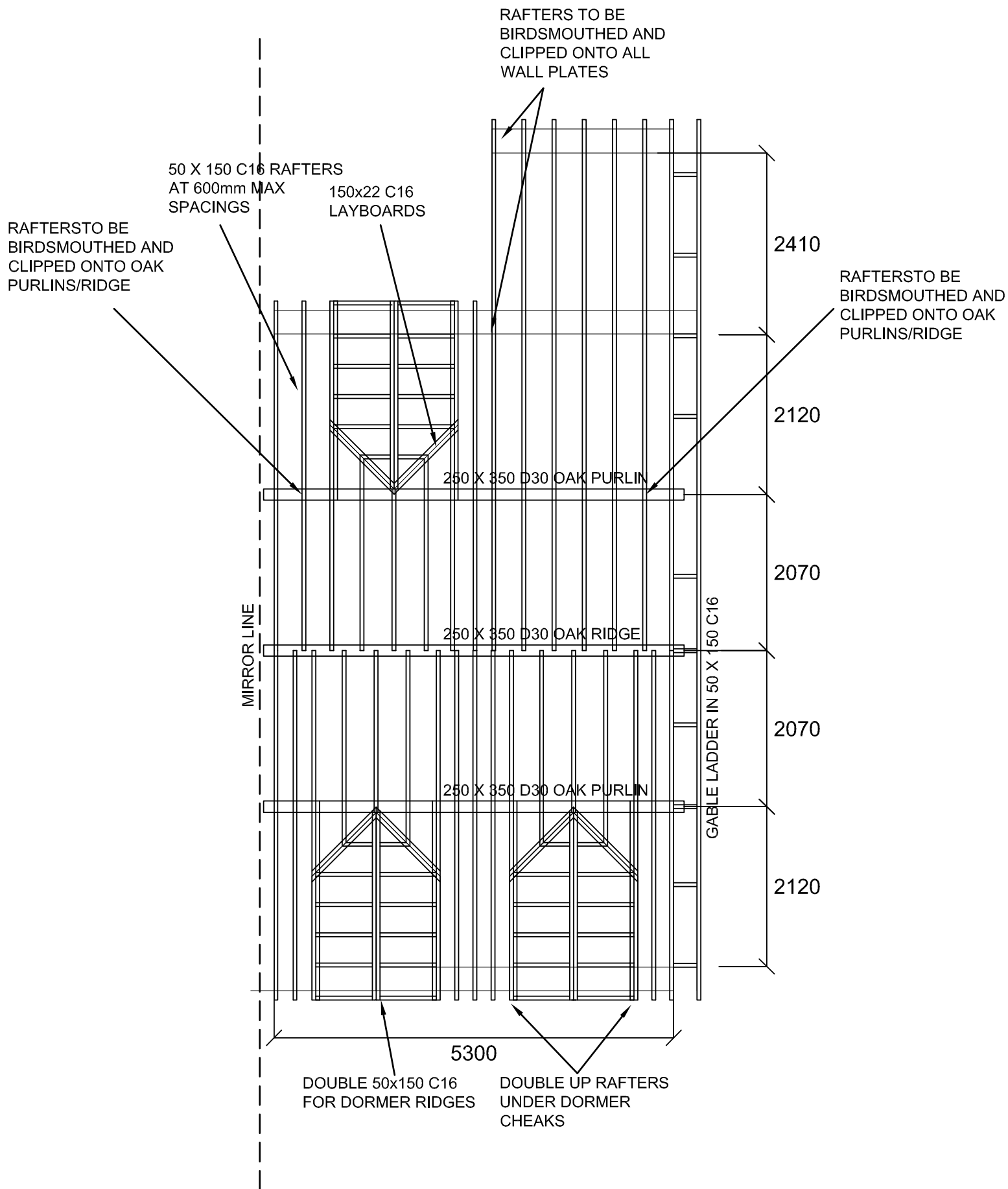
Total final deflection

$$\delta_{fin} = \delta_{finG} + \delta_{finQ} = \mathbf{12.570 \text{ mm}}$$

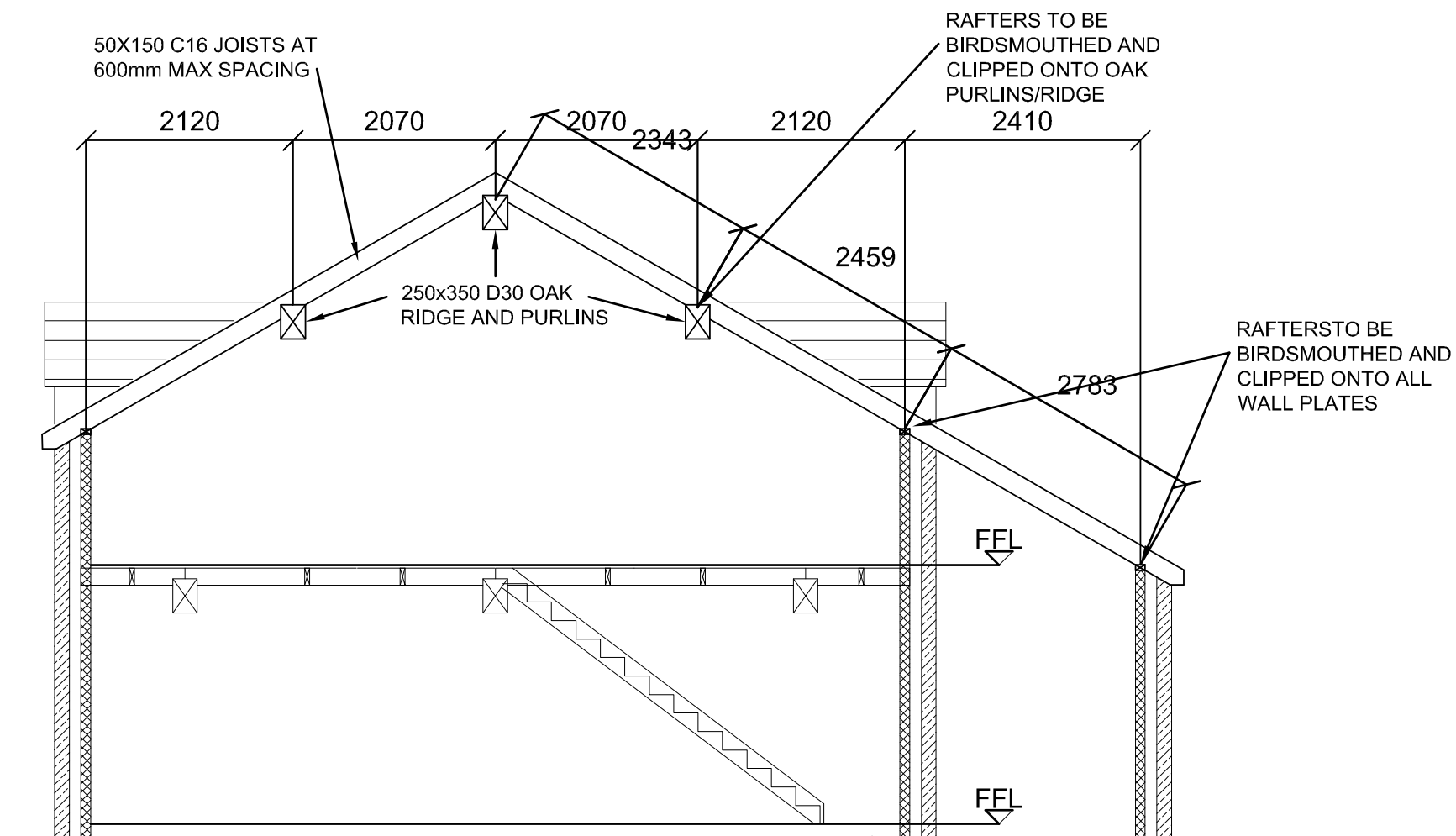
$$\delta_{fin} / \delta_{lim} = \mathbf{0.898}$$

**PASS - Total final deflection is less than the deflection limit**

**ROOF DESIGN**



**ROOF PLAN**



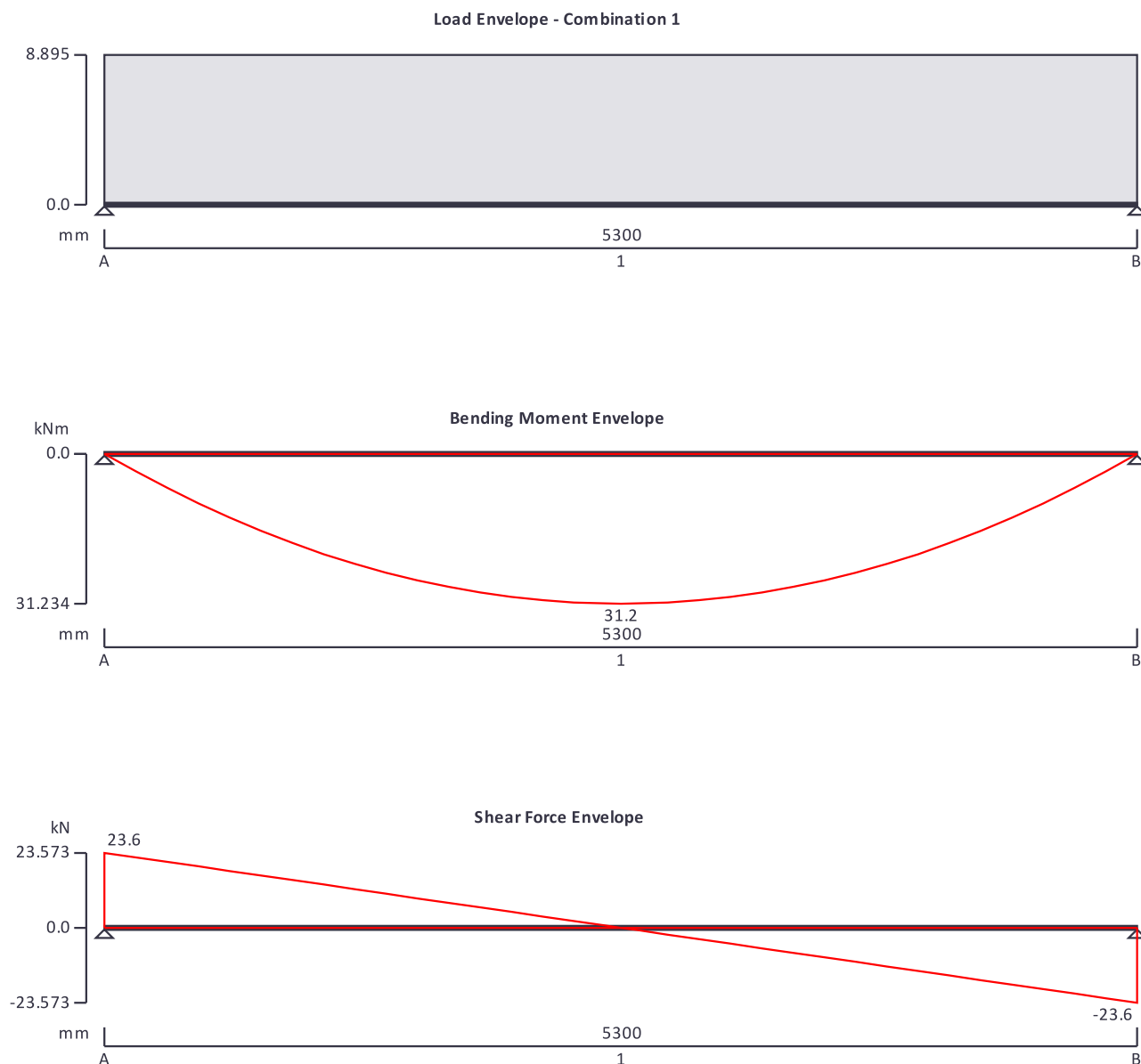
**SECTION**

Project <b>Moss Farm Cottages</b>				Job no.	
Calcs for <b>Oak Roof Purlins and Ridge</b>				Start page no./Revision <b>1</b>	
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### TIMBER BEAM ANALYSIS & DESIGN TO EN1995-1-1:2004

In accordance with EN1995-1-1:2004 + A2:2014 and Corrigendum No.1 and the UK National Annex incorporating National Amendment No.1

Tedds calculation version 1.7.04



#### Applied loading

##### Beam loads

Dead

Permanent self weight of beam \* 1

Imposed

Permanent full UDL 4.390 kN/m

Variable full UDL 1.570 kN/m

##### Load combinations

Load combination 1

Support A

Permanent \* 1.35

Variable \* 1.50

Span 1

Permanent \* 1.35

Variable \* 1.50

Support B

Permanent \* 1.35

Variable \* 1.50

##### Analysis results

Maximum moment

$M_{max} = 31.234$  kNm

$M_{min} = 0.000$  kNm

Design moment

$M = \max(\text{abs}(M_{max}), \text{abs}(M_{min})) = 31.234$  kNm

Maximum shear

$F_{max} = 23.573$  kN

$F_{min} = -23.573$  kN

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Design shear

$$F = \max(\text{abs}(F_{\max}), \text{abs}(F_{\min})) = \mathbf{23.573 \text{ kN}}$$

Total load on beam

$$W_{\text{tot}} = \mathbf{47.146 \text{ kN}}$$

Reactions at support A

$$R_{A_{\max}} = \mathbf{23.573 \text{ kN}}$$

$$R_{A_{\min}} = \mathbf{23.573 \text{ kN}}$$

Unfactored permanent load reaction at support A

$$R_{A_{\text{Permanent}}} = \mathbf{12.839 \text{ kN}}$$

Unfactored variable load reaction at support A

$$R_{A_{\text{Variable}}} = \mathbf{4.161 \text{ kN}}$$

Reactions at support B

$$R_{B_{\max}} = \mathbf{23.573 \text{ kN}}$$

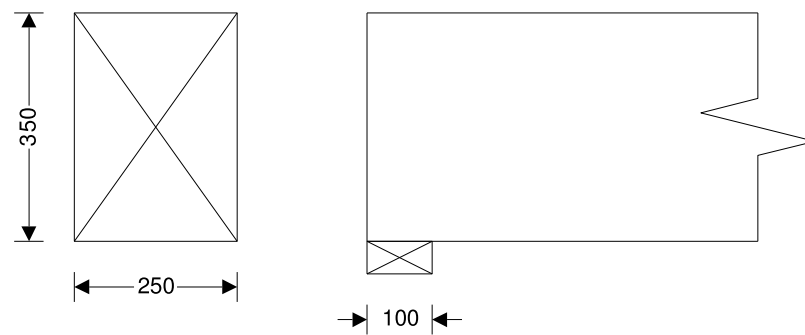
$$R_{B_{\min}} = \mathbf{23.573 \text{ kN}}$$

Unfactored permanent load reaction at support B

$$R_{B_{\text{Permanent}}} = \mathbf{12.839 \text{ kN}}$$

Unfactored variable load reaction at support B

$$R_{B_{\text{Variable}}} = \mathbf{4.161 \text{ kN}}$$



### Timber section details

Breadth of timber sections

$$b = \mathbf{250 \text{ mm}}$$

Depth of timber sections

$$h = \mathbf{350 \text{ mm}}$$

Number of timber sections in member

$$N = \mathbf{1}$$

Overall breadth of timber member

$$b_b = N \times b = \mathbf{250 \text{ mm}}$$

Timber strength class - EN 338:2016 Table 3

**D30**

### Member details

Load duration - cl.2.3.1.2

**Medium-term**

Service class of timber - cl.2.3.1.3

**1**

Length of span

$$L_{s1} = \mathbf{5300 \text{ mm}}$$

Length of bearing

$$L_b = \mathbf{100 \text{ mm}}$$

### Section properties

Cross sectional area of member

$$A = N \times b \times h = \mathbf{87500 \text{ mm}^2}$$

Section modulus

$$W_y = N \times b \times h^2 / 6 = \mathbf{5104167 \text{ mm}^3}$$

$$W_z = h \times (N \times b)^2 / 6 = \mathbf{3645833 \text{ mm}^3}$$

Second moment of area

$$I_y = N \times b \times h^3 / 12 = \mathbf{893229167 \text{ mm}^4}$$

$$I_z = h \times (N \times b)^3 / 12 = \mathbf{455729167 \text{ mm}^4}$$

Radius of gyration

$$r_y = \sqrt{I_y / A} = \mathbf{101.0 \text{ mm}}$$

$$r_z = \sqrt{I_z / A} = \mathbf{72.2 \text{ mm}}$$

### Partial factor for material properties and resistances

Partial factor for material properties - Table 2.3

$$\gamma_M = \mathbf{1.300}$$

### Modification factors

Modification factor for load duration and moisture content - Table 3.1

$$k_{\text{mod}} = \mathbf{0.800}$$

Deformation factor for service classes - Table 3.2

$$k_{\text{def}} = \mathbf{0.600}$$

Depth factor for bending - exp.3.1

$$k_{h,m} = \mathbf{1.000}$$

Depth factor for tension - exp.3.1

$$k_{h,t} = \mathbf{1.000}$$

Bending stress re-distribution factor - cl.6.1.6(2)

$$k_m = \mathbf{0.700}$$

Crack factor for shear resistance - cl.6.1.7(2)

$$k_{\text{cr}} = \mathbf{0.670}$$

Load configuration factor - exp.6.4

$$k_{c,90} = \mathbf{1.000}$$

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System strength factor - cl.6.6

$$k_{sys} = 1.000$$

Lateral buckling factor - cl.6.3.3(5)

$$k_{crit} = 1.000$$

### Compression perpendicular to the grain - cl.6.1.5

Design compressive stress

$$\sigma_{c.90.d} = R_{A\_max} / (N * b * L_b) = 0.943 \text{ N/mm}^2$$

Design compressive strength

$$f_{c.90.d} = k_{mod} * k_{sys} * k_{c.90} * f_{c.90.k} / \gamma_M = 3.262 \text{ N/mm}^2$$

$$\sigma_{c.90.d} / f_{c.90.d} = 0.289$$

**PASS - Design compressive strength exceeds design compressive stress at bearing**

### Bending - cl 6.1.6

Design bending stress

$$\sigma_{m.d} = M / W_y = 6.119 \text{ N/mm}^2$$

Design bending strength

$$f_{m.d} = k_{h.m} * k_{mod} * k_{sys} * k_{crit} * f_{m.k} / \gamma_M = 18.462 \text{ N/mm}^2$$

$$\sigma_{m.d} / f_{m.d} = 0.331$$

**PASS - Design bending strength exceeds design bending stress**

### Shear - cl.6.1.7

Applied shear stress

$$\tau_d = 3 * F / (2 * k_{cr} * A) = 0.603 \text{ N/mm}^2$$

Permissible shear stress

$$f_{v.d} = k_{mod} * k_{sys} * f_{v.k} / \gamma_M = 2.400 \text{ N/mm}^2$$

$$\tau_d / f_{v.d} = 0.251$$

**PASS - Design shear strength exceeds design shear stress**

### Deflection - cl.7.2

Deflection limit

$$\delta_{lim} = \min(14 \text{ mm}, 0.004 * L_{s1}) = 14.000 \text{ mm}$$

Instantaneous deflection due to permanent load

$$\delta_{instG} = 5.404 \text{ mm}$$

Final deflection due to permanent load

$$\delta_{finG} = \delta_{instG} * (1 + k_{def}) = 8.647 \text{ mm}$$

Instantaneous deflection due to variable load

$$\delta_{instQ} = 1.751 \text{ mm}$$

Factor for quasi-permanent variable action

$$\psi_2 = 0.3$$

Final deflection due to variable load

$$\delta_{finQ} = \delta_{instQ} * (1 + \psi_2 * k_{def}) = 2.066 \text{ mm}$$

Total final deflection

$$\delta_{fin} = \delta_{finG} + \delta_{finQ} = 10.713 \text{ mm}$$

$$\delta_{fin} / \delta_{lim} = 0.765$$

**PASS - Total final deflection is less than the deflection limit**

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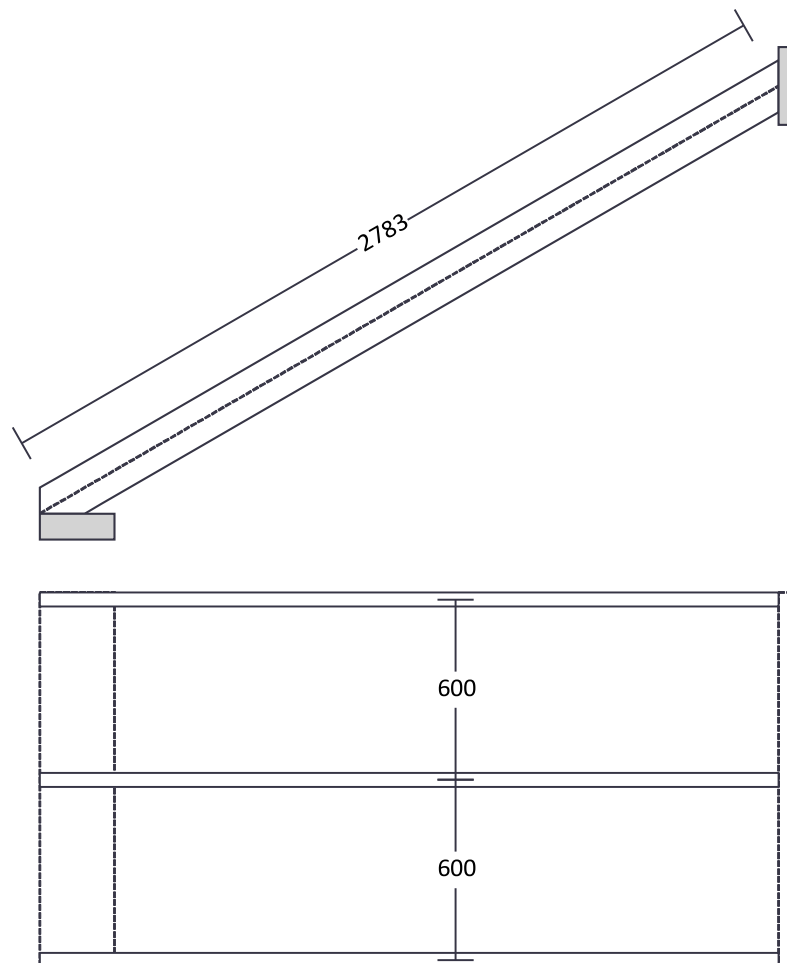
### TIMBER RAFTER ANALYSIS & DESIGN (EN1995-1-1:2004)

In accordance with EN1995-1-1:2004 + A2:2014 incorporating corrigendum June 2006 and the UK national annex

Tedds calculation version 1.0.04

#### Rafter details

Description 47 x 150 C16 timber rafters  
Rafter spacing  $S_{\text{Rafter}} = 600$  mm  
Rafter inclination  $\theta_{\text{Rafter}} = 30$  deg



#### Forces input on Rafter

Permanent load on slope  $F_{G\_Rafter} = 1.10$  kN/m<sup>2</sup>

Snow load on plan  $F_{S\_Rafter} = 0.75$  kN/m<sup>2</sup>

#### Rafter loading details

##### Distributed loads

Permanent load on slope  $p_G = F_{G\_Rafter} * S_{\text{Rafter}} = 0.66$  kN/m

Snow load on slope  $p_S = F_{S\_Rafter} * S_{\text{Rafter}} * \cos(\theta_{\text{Rafter}}) = 0.39$  kN/m

### ANALYSIS

Tedds calculation version 1.0.35

#### Loading

Self weight included (Permanent x 1)

#### Load combination factors

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Load combination	Permanent	Imposed	Snow	Wind
1.35G + 1.50Q (Strength)	1.35	1.50	0.00	0.00
1.00G + 1.00Q (Service)	1.00	1.00	0.00	0.00

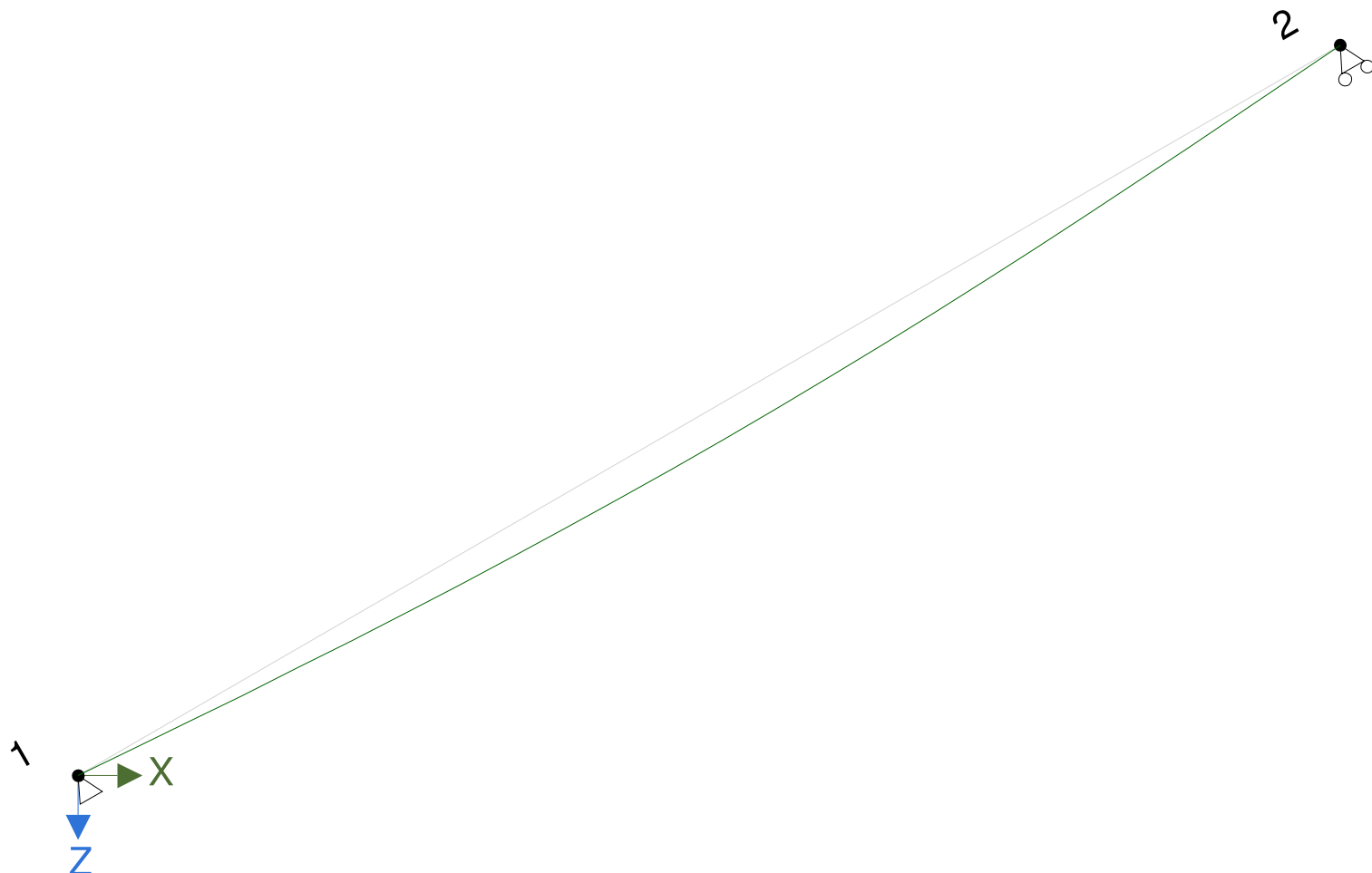
**Member Loads**

Member	Load case	Load Type	Orientation	Description
Member	Permanent	UDL	GlobalZ	0.66 kN/m at 0 m to 2.783 m
Member	Snow	UDL	GlobalZ	0.39 kN/m at 0 m to 2.783 m

**Results**

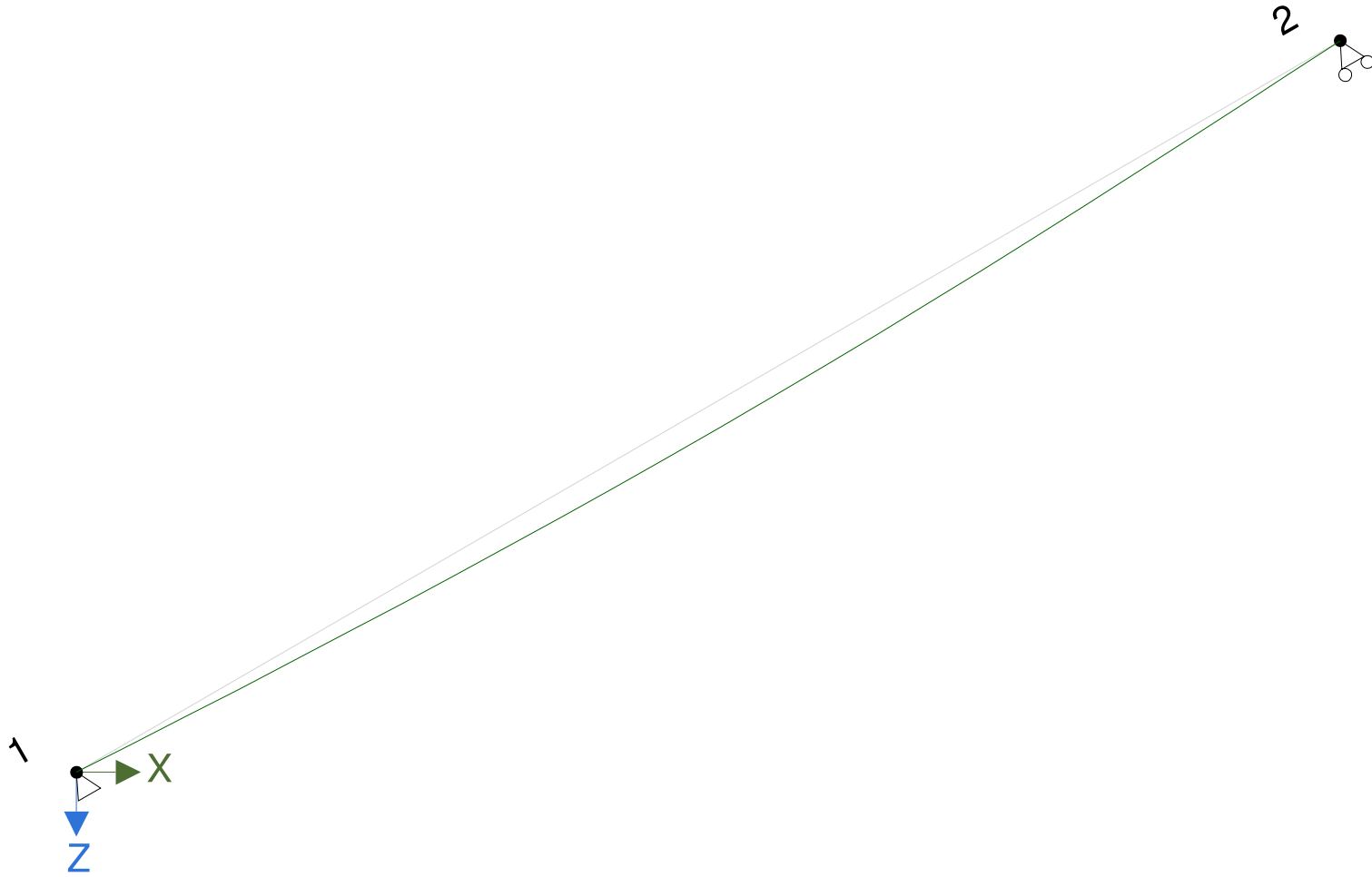
**Total deflection**

**1.35G + 1.50Q (Strength) - Total deflection**



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				3	
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**1.00G + 1.00Q (Service) - Total deflection**



**Node deflections**

**Load combination: 1.35G + 1.50Q (Strength)**

Node	Deflection		Rotation (°)	Co-ordinate system
	X (mm)	Z (mm)		
1	0	0	0.38767	Member
2	0	0	-0.38767	Member

**Load combination: 1.00G + 1.00Q (Service)**

Node	Deflection		Rotation (°)	Co-ordinate system
	X (mm)	Z (mm)		
1	0	0	0.28716	Member
2	0	0	-0.28716	Member

**Total base reactions**

Load case/combination	Force	
	FX (kN)	FZ (kN)
1.35G + 1.50Q (Strength)	0	2.6
1.00G + 1.00Q (Service)	0	1.9

**Element end forces**

**Load combination: 1.35G + 1.50Q (Strength)**

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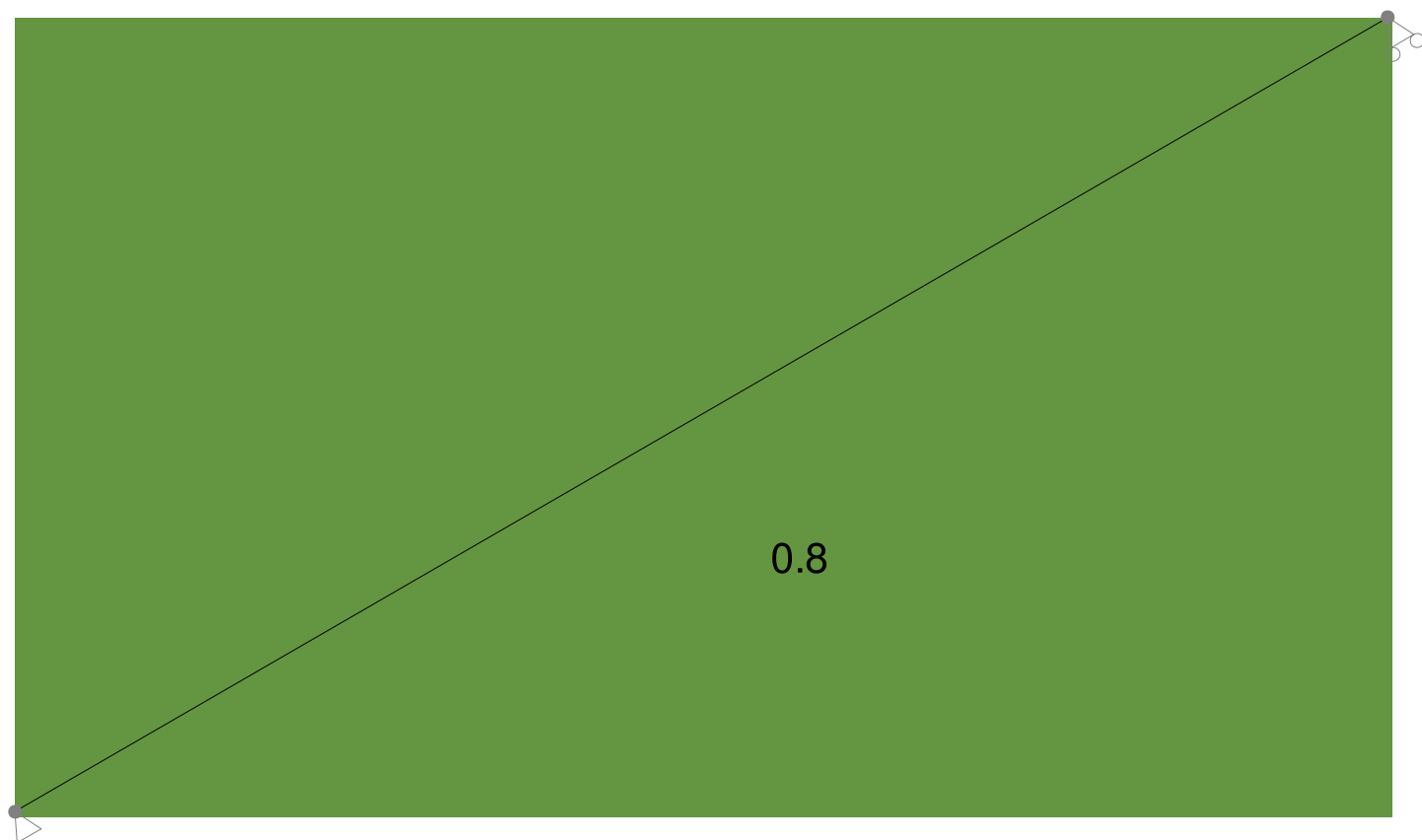
Element	Length (m)	Nodes Start/End	Axial force (kN)	Shear force (kN)	Moment (kNm)
1	2.783	1	-1.3	-1.1	0
		2	0	-1.1	0

Load combination: 1.00G + 1.00Q (Service)

Element	Length (m)	Nodes Start/End	Axial force (kN)	Shear force (kN)	Moment (kNm)
1	2.783	1	-0.9	-0.8	0
		2	0	-0.8	0

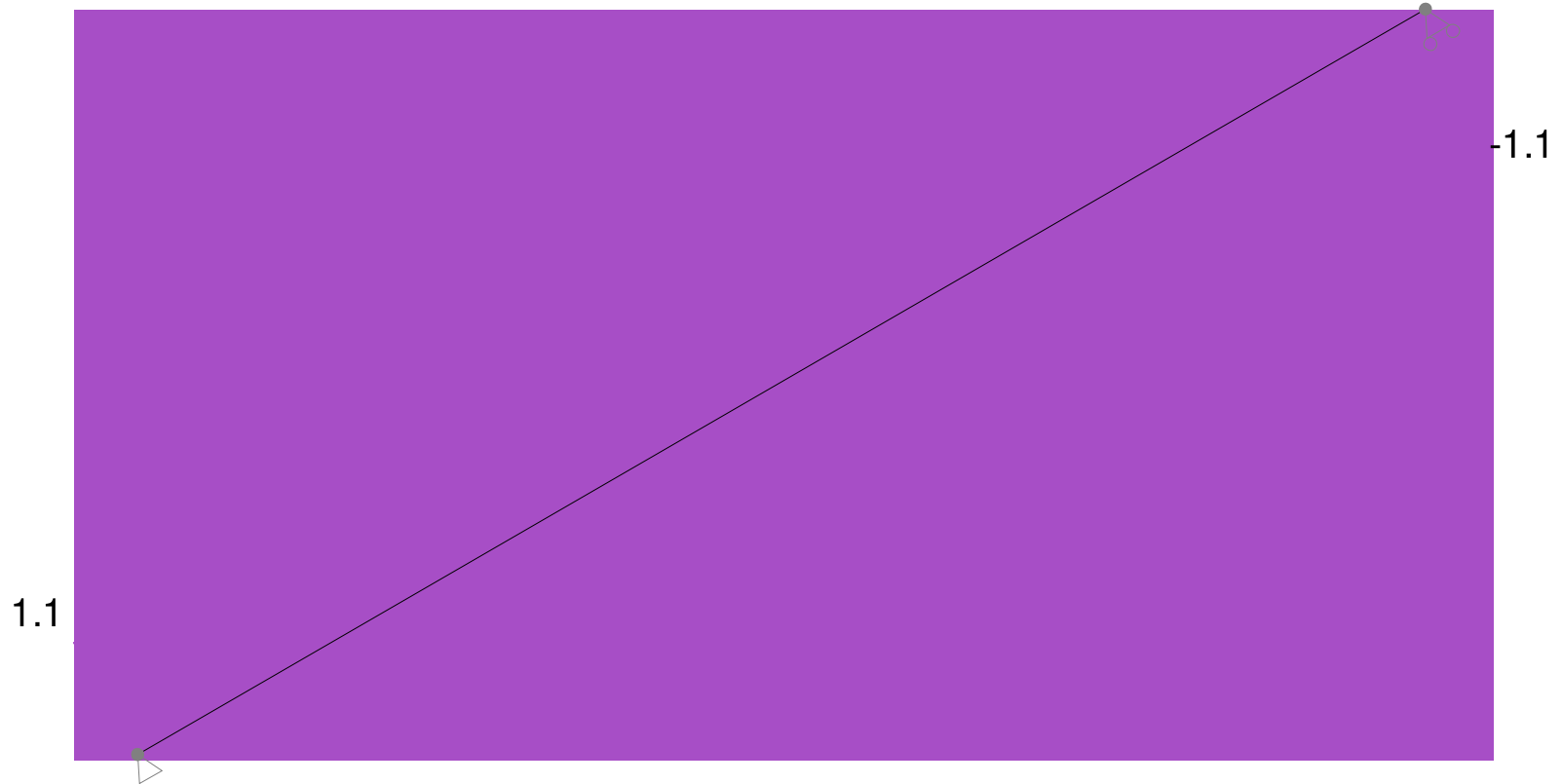
**Forces**

**Strength combinations - Moment envelope (kNm)**



Project Moss Farm Cottages				Job no.	
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### Strength combinations - Shear envelope (kN)



#### Member results

##### Envelope - Strength combinations

Member	Position (m)	Shear force (kN)	Moment (kNm)
Member	0	1.1 (max abs)	0 (min)
	1.392	0	0.8 (max)
	2.783	-1.1	0 (min)

Tedds calculation version 2.2.07

#### Member - Span 1

##### Partial factor for material properties and resistances

Partial factor for material properties - Table 2.3  $\gamma_M = 1.300$

##### Member details

Load duration - cl.2.3.1.2 Medium-term

Service class - cl.2.3.1.3 2

##### Timber section details

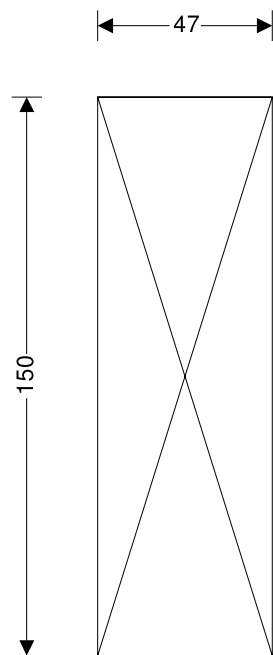
Number of timber sections in member N = 1

Breadth of sections b = 47 mm

Depth of sections h = 150 mm

Timber strength class - EN 338:2016 Table 1 C16

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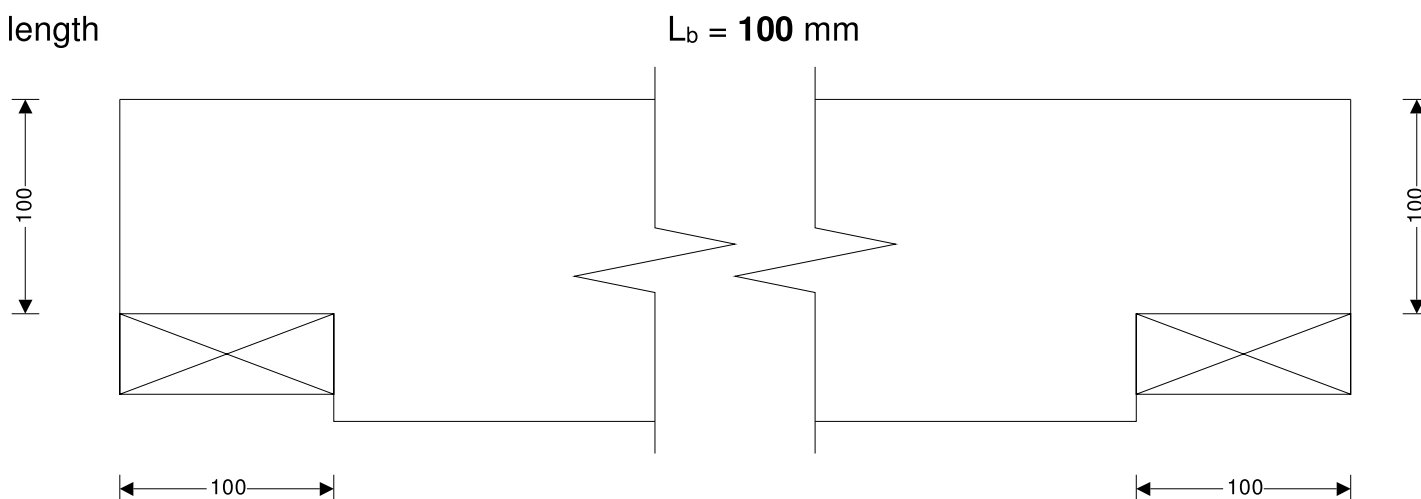


**47x150 timber section**

Cross-sectional area,  $A$ , 7050 mm<sup>2</sup>  
Section modulus,  $W_y$ , 176250 mm<sup>3</sup>  
Section modulus,  $W_z$ , 55225 mm<sup>3</sup>  
Second moment of area,  $I_y$ , 13218750 mm<sup>4</sup>  
Second moment of area,  $I_z$ , 1297787 mm<sup>4</sup>  
Radius of gyration,  $i_y$ , 43.3 mm  
Radius of gyration,  $i_z$ , 13.6 mm  
**Timber strength class C16**  
Characteristic bending strength,  $f_{m,k}$ , 16 N/mm<sup>2</sup>  
Characteristic shear strength,  $f_{v,k}$ , 3.2 N/mm<sup>2</sup>  
Characteristic compression strength parallel to grain,  $f_{c,0,k}$ , 17 N/mm<sup>2</sup>  
Characteristic compression strength perpendicular to grain,  $f_{c,90,k}$ , 2.2 N/mm<sup>2</sup>  
Characteristic tension strength parallel to grain,  $f_{t,0,k}$ , 8.5 N/mm<sup>2</sup>  
Mean modulus of elasticity,  $E_{0,mean}$ , 8000 N/mm<sup>2</sup>  
Fifth percentile modulus of elasticity,  $E_{0,05}$ , 5400 N/mm<sup>2</sup>  
Shear modulus of elasticity,  $G_{mean}$ , 500 N/mm<sup>2</sup>  
Characteristic density,  $\rho_k$ , 310 kg/m<sup>3</sup>  
Mean density,  $\rho_{mean}$ , 370 kg/m<sup>3</sup>

**Span details**

Bearing length



**Consider Combination 1 - 1.35G + 1.50Q (Strength)**

**Modification factors**

Duration of load and moisture content - Table 3.1  $k_{mod} = 0.8$   
Deformation factor - Table 3.2  $k_{def} = 0.8$   
Bending stress re-distribution factor - cl.6.1.6(2)  $k_m = 0.7$   
Crack factor for shear resistance - cl.6.1.7(2)  $k_{cr} = 0.67$   
System strength factor - cl.6.6  $k_{sys} = 1.1$   
Notch reduction factor - exp.6.61  $k_v = 1$

**Check compression parallel to the grain - cl.6.1.4**

Design axial compression  $P_d = 1.28$  kN  
Design compressive stress  $\sigma_{c,0,d} = P_d / A = 0.182$  N/mm<sup>2</sup>  
Design compressive strength  $f_{c,0,d} = k_{mod} * k_{sys} * f_{c,0,k} / \gamma_M = 11.508$  N/mm<sup>2</sup>  
 $\sigma_{c,0,d} / f_{c,0,d} = 0.016$

**PASS - Design parallel compression strength exceeds design parallel compression stress**

**Check design at start of span**

**Check shear force - Section 6.1.7**

Design shear force  $F_{y,d} = 1.109$  kN  
Design shear stress - exp.6.60  $\tau_{y,d} = 1.5 * F_{y,d} / (k_{cr} * b * h) = 0.352$  N/mm<sup>2</sup>

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Design shear strength

$$f_{v,y,d} = k_{mod} * k_{sys} * f_{v,k} / \gamma_M = \mathbf{2.166 \text{ N/mm}^2}$$

$$\tau_{y,d} / f_{v,y,d} = \mathbf{0.163}$$

**PASS - Design shear strength exceeds design shear stress**

**Check columns subjected to either compression or combined compression and bending - cl.6.3.2**

Effective length for y-axis bending

$$L_{e,y} = 0.9 * 2783 \text{ mm} = \mathbf{2505 \text{ mm}}$$

Slenderness ratio

$$\lambda_y = L_{e,y} / i_y = \mathbf{57.844}$$

Relative slenderness ratio - exp. 6.21

$$\lambda_{rel,y} = \lambda_y / \pi * \sqrt{(f_{c,0,k} / E_{0.05})} = \mathbf{1.033}$$

Effective length for z-axis bending

$$L_{e,z} = \mathbf{0 \text{ mm}}$$

Slenderness ratio

$$\lambda_z = L_{e,z} / i_z = \mathbf{0}$$

Relative slenderness ratio - exp. 6.22

$$\lambda_{rel,z} = \lambda_z / \pi * \sqrt{(f_{c,0,k} / E_{0.05})} = \mathbf{0}$$

**$\lambda_{rel,y} > 0.3$  column stability check is required**

Straightness factor

$$\beta_c = \mathbf{0.2}$$

Instability factors - exp.6.25, 6.26, 6.27 & 6.28

$$k_y = 0.5 * (1 + \beta_c * (\lambda_{rel,y} - 0.3) + \lambda_{rel,y}^2) = \mathbf{1.107}$$

$$k_z = 0.5 * (1 + \beta_c * (\lambda_{rel,z} - 0.3) + \lambda_{rel,z}^2) = \mathbf{0.470}$$

$$k_{c,y} = 1 / (k_y + \sqrt{(k_y^2 - \lambda_{rel,y}^2)}) = \mathbf{0.665}$$

$$k_{c,z} = 1 / (k_z + \sqrt{(k_z^2 - \lambda_{rel,z}^2)}) = \mathbf{1.064}$$

Column stability checks - exp.6.23 & 6.24

$$\sigma_{c,0,d} / (k_{c,y} * f_{c,0,d}) = \mathbf{0.024}$$

$$\sigma_{c,0,d} / (k_{c,z} * f_{c,0,d}) = \mathbf{0.015}$$

**PASS - Column stability is acceptable**

**Check design 1392 mm along span**

**Check bending moment - Section 6.1.6**

Design bending moment

$$M_{y,d} = \mathbf{0.771 \text{ kNm}}$$

Design bending stress

$$\sigma_{m,y,d} = M_{y,d} / W_y = \mathbf{4.376 \text{ N/mm}^2}$$

Design bending strength

$$f_{m,y,d} = k_{mod} * k_{sys} * f_{m,k} / \gamma_M = \mathbf{10.831 \text{ N/mm}^2}$$

$$\sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.404}$$

**PASS - Design bending strength exceeds design bending stress**

**Check combined bending and axial compression - Section 6.2.4**

Combined loading checks - exp.6.19 & 6.20

$$(\sigma_{c,0,d} / f_{c,0,d})^2 + \sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.404}$$

$$(\sigma_{c,0,d} / f_{c,0,d})^2 + k_m * \sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.283}$$

**PASS - Combined bending and axial compression utilisation is acceptable**

**Check columns subjected to either compression or combined compression and bending - cl.6.3.2**

Effective length for y-axis bending

$$L_{e,y} = 0.9 * 2783 \text{ mm} = \mathbf{2505 \text{ mm}}$$

Slenderness ratio

$$\lambda_y = L_{e,y} / i_y = \mathbf{57.844}$$

Relative slenderness ratio - exp. 6.21

$$\lambda_{rel,y} = \lambda_y / \pi * \sqrt{(f_{c,0,k} / E_{0.05})} = \mathbf{1.033}$$

Effective length for z-axis bending

$$L_{e,z} = \mathbf{0 \text{ mm}}$$

Slenderness ratio

$$\lambda_z = L_{e,z} / i_z = \mathbf{0}$$

Relative slenderness ratio - exp. 6.22

$$\lambda_{rel,z} = \lambda_z / \pi * \sqrt{(f_{c,0,k} / E_{0.05})} = \mathbf{0}$$

**$\lambda_{rel,y} > 0.3$  column stability check is required**

Straightness factor

$$\beta_c = \mathbf{0.2}$$

Instability factors - exp.6.25, 6.26, 6.27 & 6.28

$$k_y = 0.5 * (1 + \beta_c * (\lambda_{rel,y} - 0.3) + \lambda_{rel,y}^2) = \mathbf{1.107}$$

$$k_z = 0.5 * (1 + \beta_c * (\lambda_{rel,z} - 0.3) + \lambda_{rel,z}^2) = \mathbf{0.470}$$

$$k_{c,y} = 1 / (k_y + \sqrt{(k_y^2 - \lambda_{rel,y}^2)}) = \mathbf{0.665}$$

$$k_{c,z} = 1 / (k_z + \sqrt{(k_z^2 - \lambda_{rel,z}^2)}) = \mathbf{1.064}$$

Column stability checks - exp.6.23 & 6.24

$$\sigma_{c,0,d} / (k_{c,y} * f_{c,0,d}) + \sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.428}$$

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$$\sigma_{c,0,d} / (k_{c,z} * f_{c,0,d}) + k_m * \sigma_{m,y,d} / f_{m,y,d} = \mathbf{0.298}$$

**PASS - Column stability is acceptable**

**Consider Combination 2 - 1.00G + 1.00Q (Service)**

**Check design 1392 mm along span**

**Check y-y axis deflection - Section 7.2**

Instantaneous deflection

$$\delta_y = \mathbf{4.6 \text{ mm}}$$

Allowable deflection

$$\delta_{y,Allowable} = L_{m1\_s1} / 250 = \mathbf{11.1 \text{ mm}}$$

$$\delta_y / \delta_{y,Allowable} = \mathbf{0.409}$$

**PASS - Allowable deflection exceeds final deflection**